

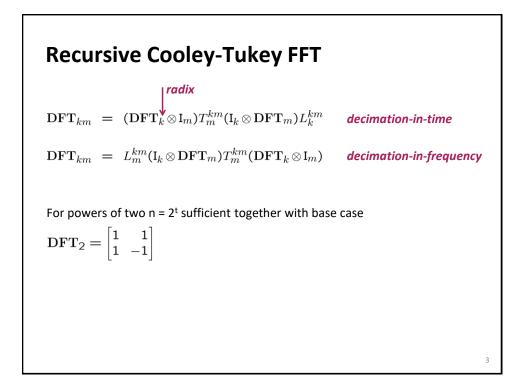
Fast FFT: Example FFTW Library

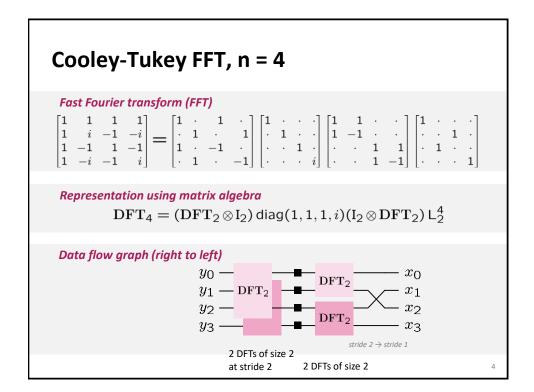
www.fftw.org

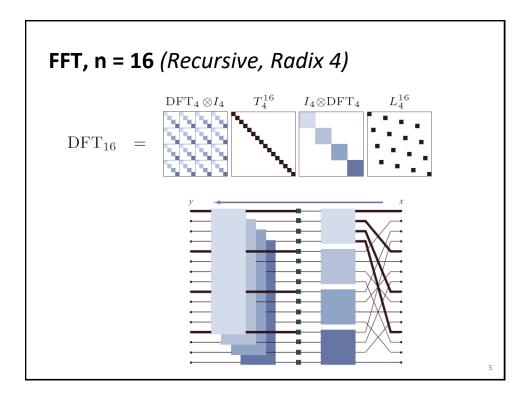
Frigo and Johnson, FFTW: An Adaptive Software Architecture for the FFT, ICASSP 1998

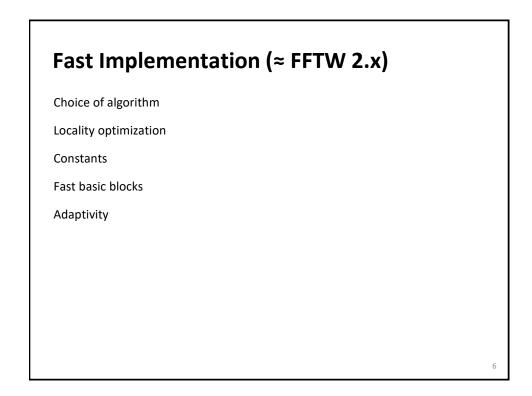
Frigo, A Fast Fourier Transform Compiler, PLDI 1999

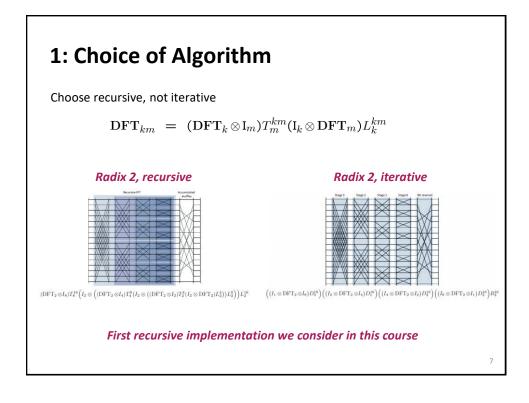
Frigo and Johnson, The Design and Implementation of FFTW3, Proc. IEEE 93(2) 2005

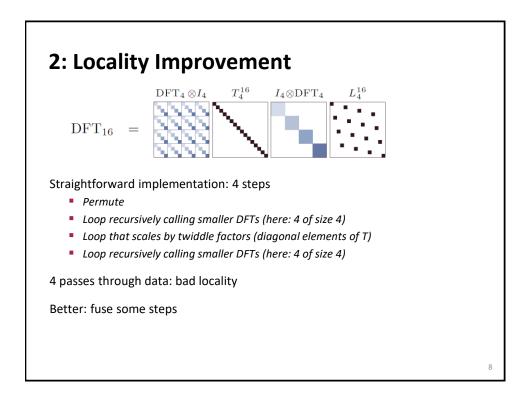


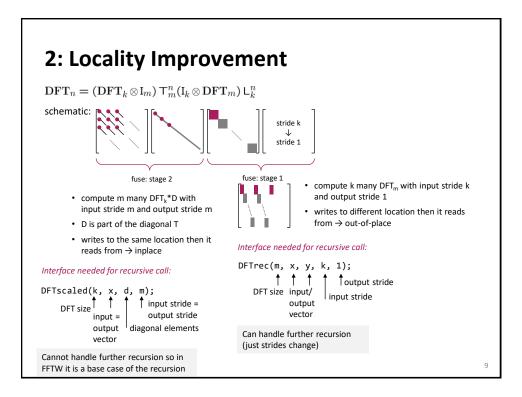


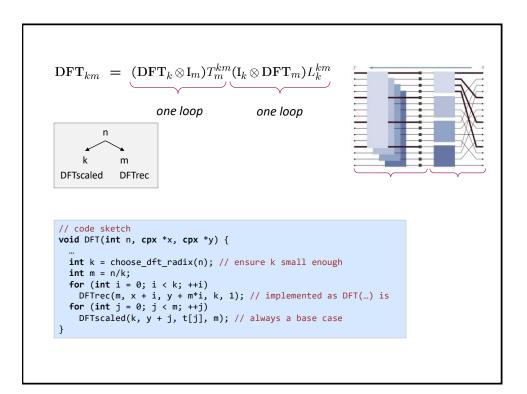




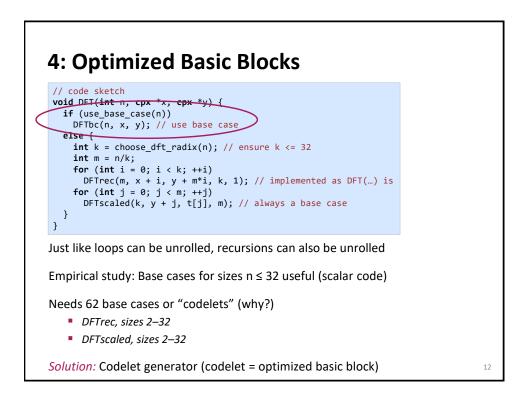


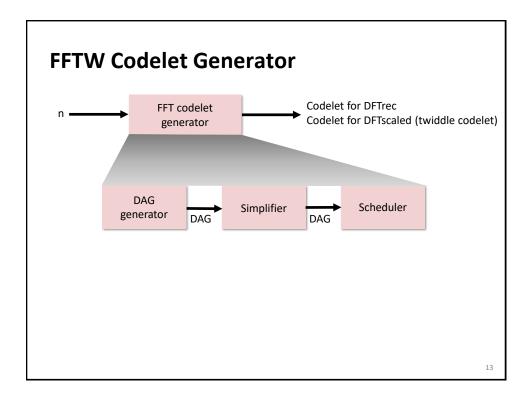


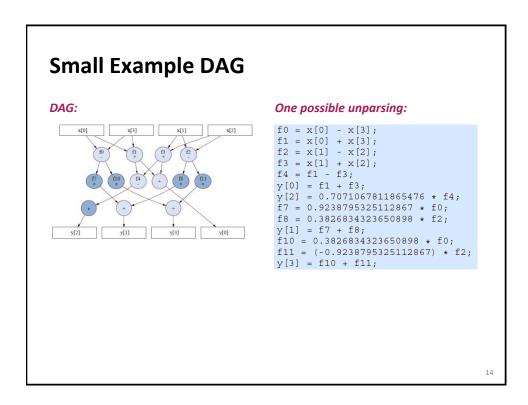


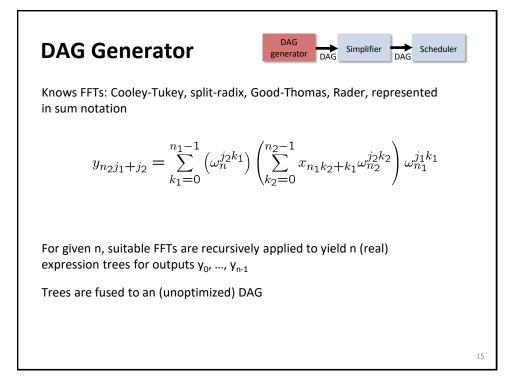


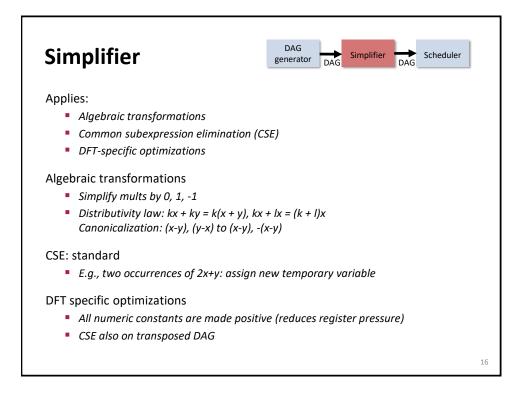
3: Constants FFT incurs multiplications by roots of unity					
FFT incurs multiplications by roots of unity	Æ				
Multiplications by sines and cosines, e.g.,	•				
y[i] = sin(i·pi/128)*x[i];					
Very expensive! <i>Observation:</i> Constants depend only on input size, not on input					
Solution: Precompute once and use many times					
<pre>d = DFT_init(1024); // init function computes constant table d(x, y); // use many times</pre>					
	11				

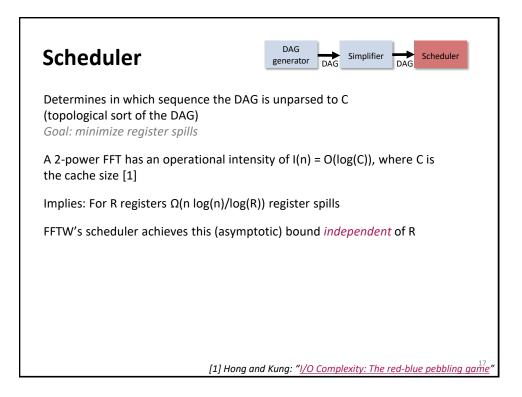


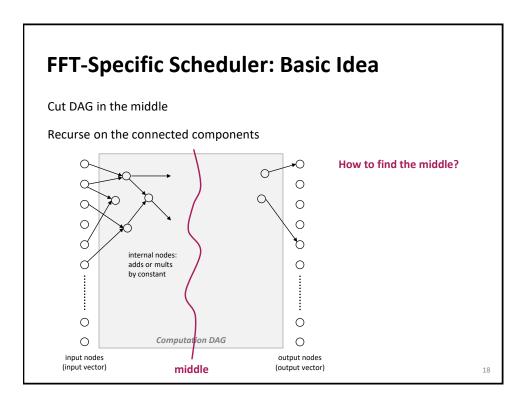


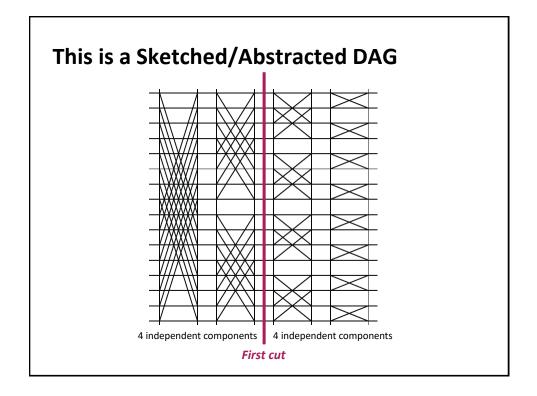


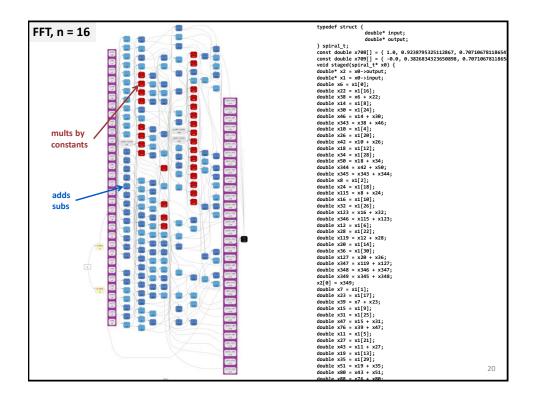












Codelet Examples

Notwiddle 2 (DFTrec)

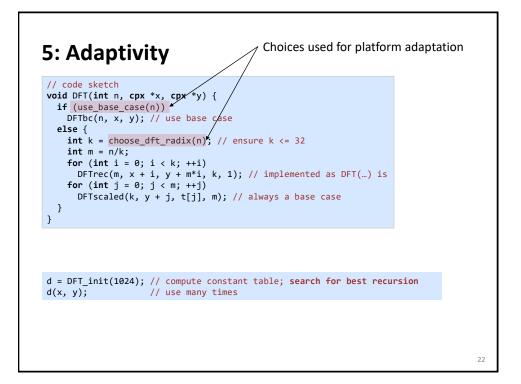
Notwiddle 3 (DFTrec)

Twiddle 3 (DFTscaled)

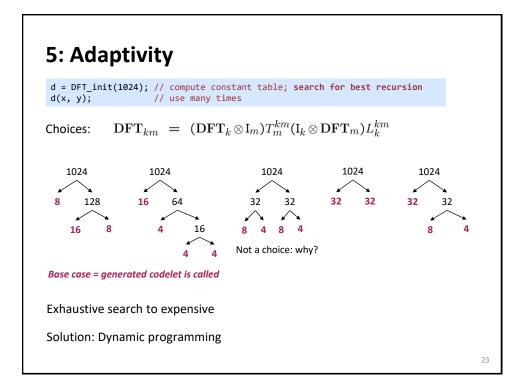
Notwiddle 32 (DFTrec)

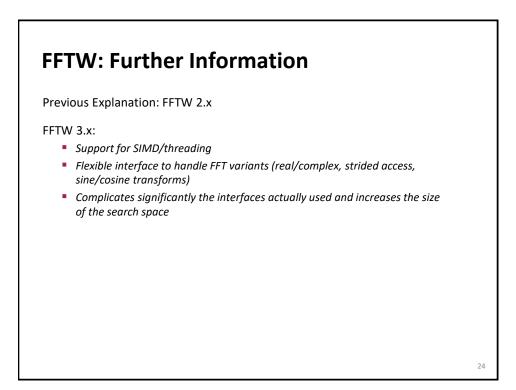
Code style:

- Single static assignment (SSA)
- Scoping (limited scope where variables are defined)



21





	MMM Atlas	Sparse MVM Sparsity/Bebop	DFT FFTW
Cache optimization			
Register optimization			
Optimized basic blocks			
Other optimizations			
Adaptivity			

	MMM Atlas	Sparse MVM Sparsity/Bebop	DFT FFTW	
Cache optimization	Blocking	Blocking (rarely useful)	Recursive FFT, fusion of steps	
Register optimization	Blocking	Blocking (changes sparse format)	Scheduling of small FFTs	
Optimized basic blocks	Unrolling, scalar replacement and SSA, scheduling, simplifications (for FFT)			
Other optimizations	-	_	Precomputation of constants	
Adaptivity	Search: blocking parameters	Search: register blocking size	Search: recursion strategy	