Advanced Systems Lab

Spring 2021 Lecture: Memory bound computation, sparse linear algebra, OSKI

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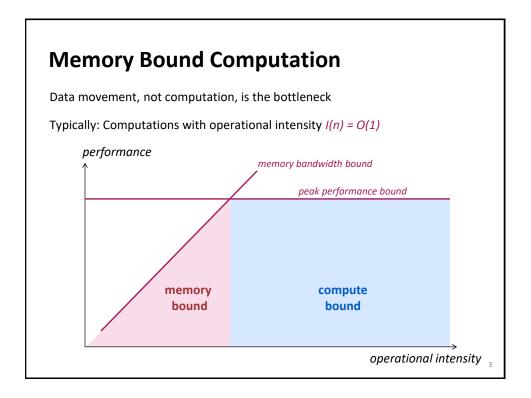
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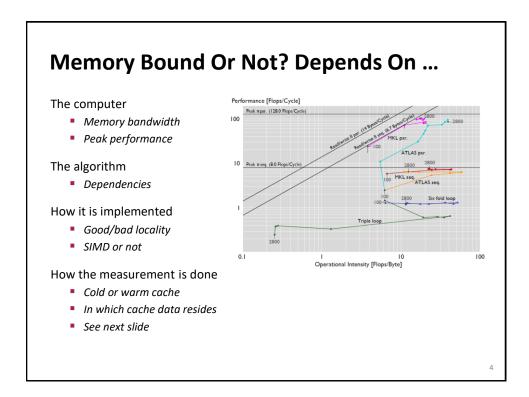
Overview

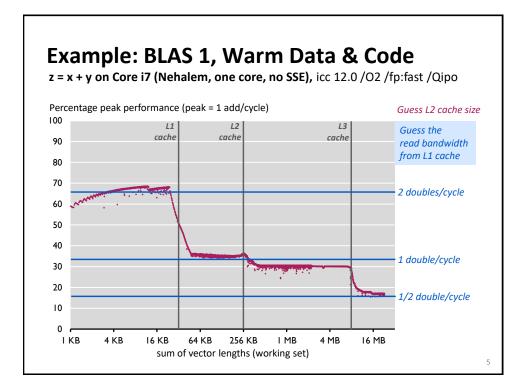
Memory bound computations

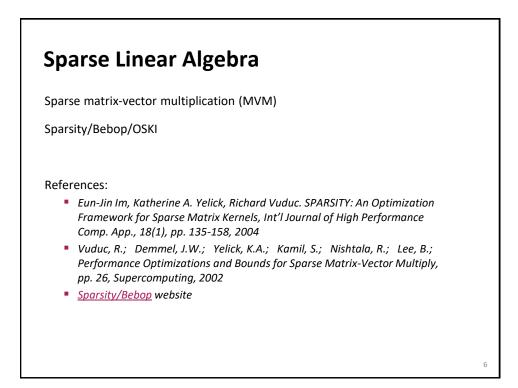
Sparse linear algebra, OSKI

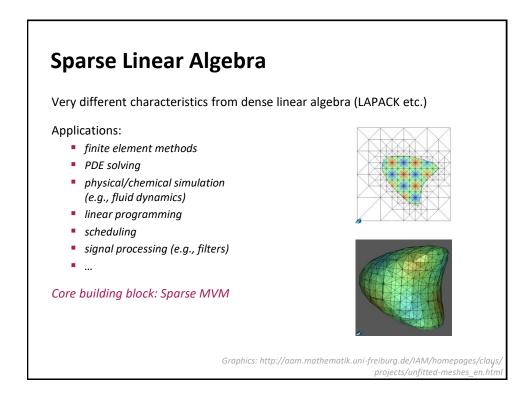
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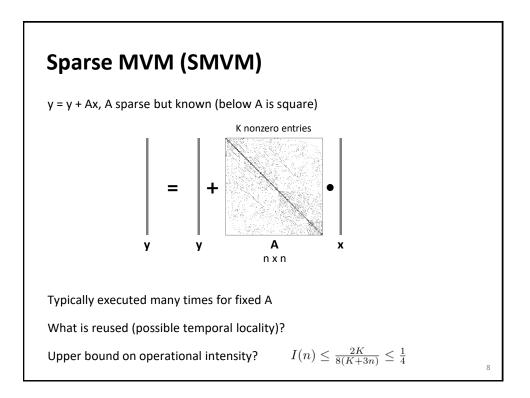


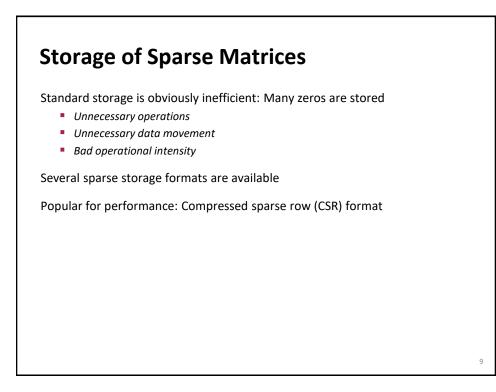


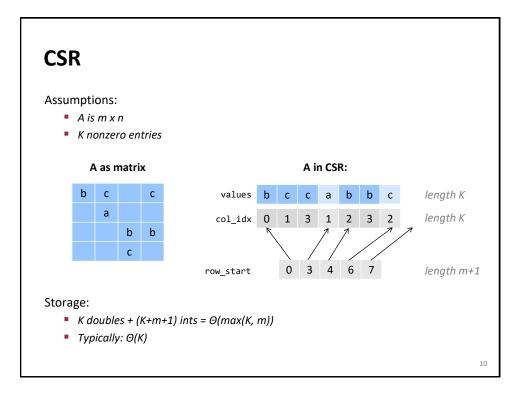












Sparse MVM Using CSR

```
y = y + Ax
```

```
int i, j;
double d;
```

```
/* loop over m rows */
for (i = 0; i < m; i++) {
    d = y[i]; /* scalar replacement since reused */</pre>
```

```
/* loop over non-zero elements in row i */
for (j = row_start[i]; j < row_start[i+1]; j++)
    d += values[j] * x[col_idx[j]];
y[i] = d;</pre>
```

CSR + sparse MVM: Advantages?

CSR

} }

Advantages:

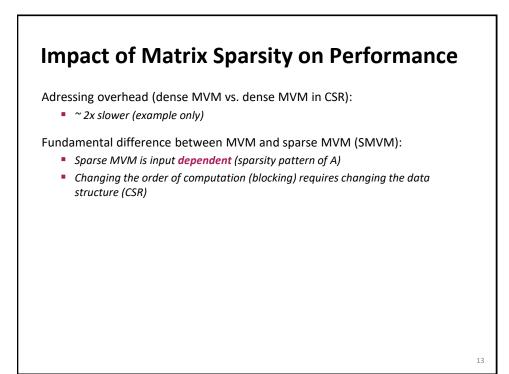
- Only nonzero values are stored
- All three arrays for A (values, col_idx, row_start) accessed consecutively in MVM (good spatial locality)
- Good temporal locality with respect to y

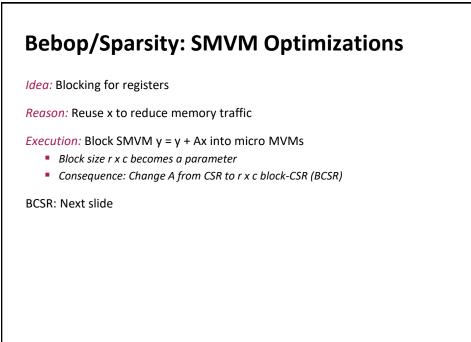
Disadvantages:

- Insertion into A is costly
- Poor temporal locality with respect to x

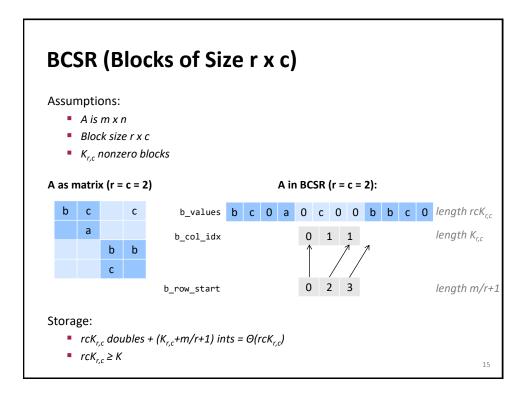
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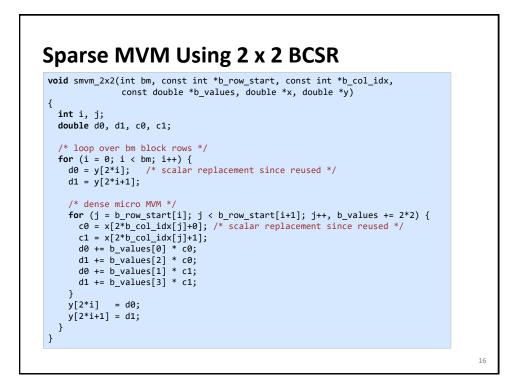
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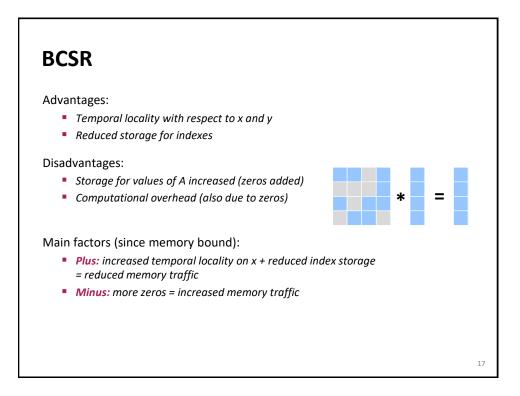


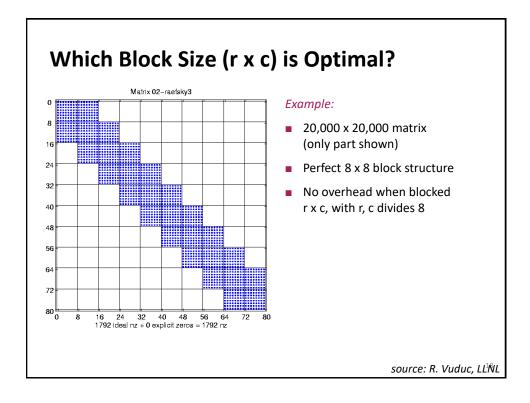


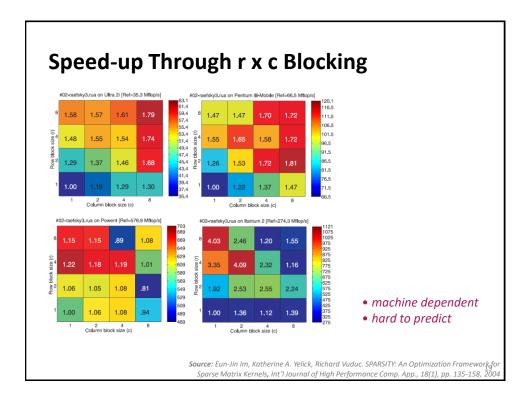
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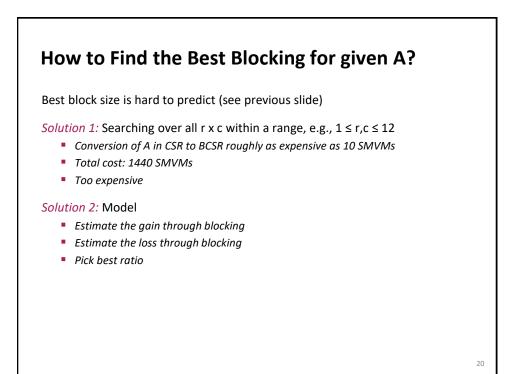




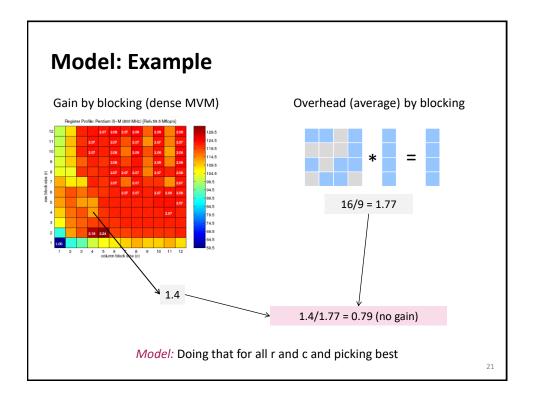


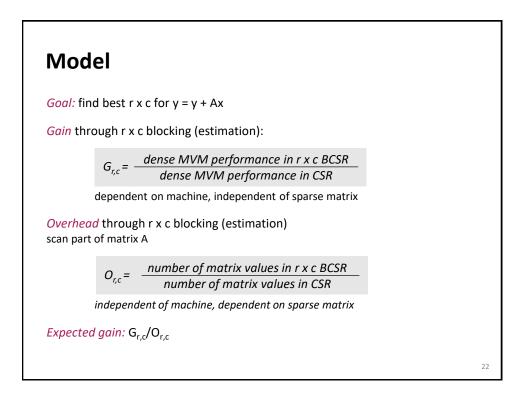


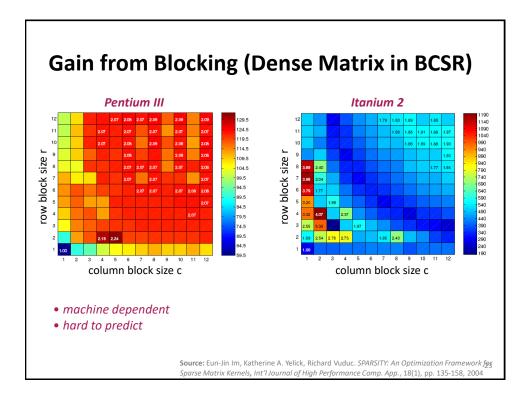


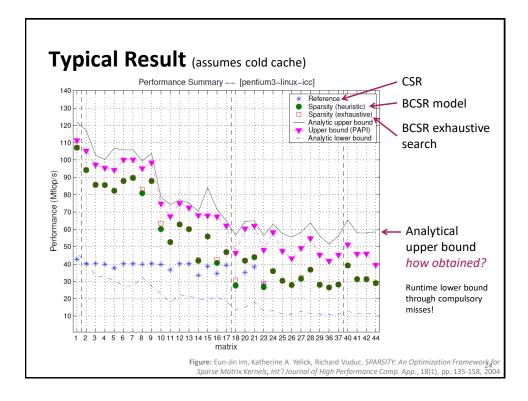


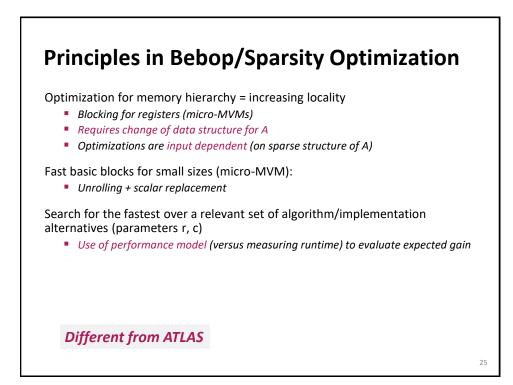
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SMVM: Other Ideas

- Cache blocking
- Value compression
- Index compression
- Pattern-based compression
- Special scenario: Multiple inputs

